# Automatic Verification of Real-Time Systems with Rich Data

Ernst-Rüdiger Olderog



RTS+D - p.1/59

# **Motivation**

#### Embedded system =

# system where computer is invisible part of it to control its function



ECUs on board of a cars: Mercedes S class (1998)

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#### Embedded system =

# system where computer is invisible part of it to control its function



ECUs on board of a cars: Mercedes S class (1998)

#### **Safety-critical** applications :

malfunction of computer is costly and dangerous

#### **Trains**

ETCS (European Train Control System) Level 3:



Safety Property: Collision Freedom

#### **Planes**

TCAS (Traffic Alert and Collision Avoidance System):



#### case of two aircrafts

# **Real-Time Systems**

... are reactive systems where certain inputs require the corresponding outputs within given time bounds.

**Example:** European Train Control System (ETCS)



Safety Property: Collision Freedom

# **AVACS Project Group R**

... advances the

automatic verification and analysis of real-time systems in three complementary projects R1–R3:

- R1: Beyond Timed Automata high-level specifications: real-time and complex infinite data
- R2: Timing Analysis, Scheduling, and Distribution of Real-Time Tasks implementation level: complex target architectures
- R3: Heuristic Search and Abstract Model Checking for Real-Time Systems highly concurrent systems: many clocks and many components

# **R1: Beyond Timed Automata**

E.-R. Olderog,

B. Finkbeiner, M. Fränzle, A. Podelski, V. Sofronie-Stokkermans

... investigates Real-Time Systems with Rich Data:

- System specification language: CSP-OZ-DC
   integrates processes (Comm. Sequ. Processes)
   data (Object-Z)
   time (Duration Calculus)
- Real-time requirements:

DC

Problem: Does specification satisfy requirement?

# **Specification of Processes**

- CSP Communicating Sequential Processes since 1978: Hoare, Brookes, Roscoe
  - synchronous communication via channels:



- parallel composition and hiding
- mathematical theory

# **Specification of Data**

- Z since 1980: Abrial, Sufrin, Spivey
  - state spaces and transformations
  - mathematical tool kit
  - schema calculus



OZ Object-Z

since 1995: Duke, Rose, Smith

- class concept
- inheritance

# **Specification of Time**

- DC Duration Calculus
  since 1991: Zhou, Hoare, Ravn, Hansen
  real-time logic and calculus
  - for properties of obs : Time  $\rightarrow D$



• interval-based properties: e.g. durations

# **Parameterized Elevator**





**Object-Z** specifies state space ...

 $Min, Max : \mathbb{Z}$ Min < Max

[state space] *current* :  $\mathbb{Z}$  $goal: \mathbb{Z}$  $dir: \{-1, 0, 1\}$ 

Init goal = current = Mindir = 0

... and operations:

 $\_com\_newgoal\_$  $\Delta(goal)$  $Min \le goal' \le Max$  [nondeterminism]  $goal' \ne current$ 

... operations, cont'd:

\_\_com\_*passed*\_\_\_\_\_ Δ(*current*) *current' = current + dir* 

$$\Delta()$$

$$goal = current$$
[precondition]

**Duration Calculus** restricts timing of states and events:

• More than 3 seconds between two *passed* events:

 $\neg \diamond$  ( $\ddagger$  passed ;  $\ell \leq 3$  ;  $\ddagger$  passed)

counterexample trace:



• Event *stop* within 2 sec after reaching *goal*:

 $\neg \diamond ([current \neq goal]; ([current = goal] \land \ell \ge 2 \land \boxminus stop))$ 

counterexample trace:

 true
 current  $\neq$  goal
 current = goal
 true

  $\frown$   $l \ge 2 \longrightarrow$   $\frown$  Time

 no
 stop
 event

# **Class Elevator**

1	
CSP	chan start, passed, stop, main $\stackrel{c}{=}$ newgoal $\rightarrow$ Drive $\stackrel{c}{=}$ (passed $\rightarrow$
	Min, Max : $\mathbb{Z}$
	Min < Max
	com_ <i>newgoal</i>
07	$\Delta(goal)$
UZ	$Min \leq goal' \leq Max$
	goal' ≠ current
	_com_ <b>passed</b>
	$\Delta(current)$
	current' = current + dir

**Flevator** 

newgoal start  $\rightarrow$  Drive *Drive*) □ (*stop*  $\rightarrow$  main) Init\_\_\_\_\_ goal = current = Min current, goal :  $\mathbb{Z}$ *dir* : {-1,0,1} dir = 0\_com\_*start*\_  $\Delta(dir)$  $goal > current \Rightarrow dir' = 1$ goal < current  $\Rightarrow$  dir ' = -1 \_com\_*stop*\_\_\_\_\_  $\Delta()$ goal = current

 $\neg$   $\diamond$  ( $\ddagger$  passed ;  $\ell \leq$  3 ;  $\ddagger$  passed)

 $\neg \diamond ([current \neq goal]; ([current = goal] \land \ell \ge 2 \land \boxminus stop))$ 

# **Semantics of CSP-OZ-DC**

by translation into Phase-Event-Automata (PEA), a variant of Timed Automata due to Hoenicke (2006)

This semantics is **compositional**:

 $\mathcal{A}(COD) = \mathcal{A}(CSP) \parallel \mathcal{A}(OZ) \parallel \mathcal{A}(DC)$ 

where || synchronises on both phases and events.





 $s(p_i)$  state invariant



 $l(p_i)$  clock invariant



- $s(p_i)$  state invariant
- $I(p_i)$  clock invariant
- *guard* conditions over events, state space and time



- $s(p_i)$  state invariant
- $l(p_i)$  clock invariant
- *guard* conditions over events, state space and time
- *resets* reset of clocks



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#### **Parallel Composition:** $\mathcal{A}_1 \parallel \mathcal{A}_2$

A run is a sequence of configurations

$$\rho = \langle \ldots, (p_i, \beta_i, \gamma_i, Y_i, t_i), \ldots \rangle$$

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each one describing an interval, where

 $\rightarrow$  *p<sub>i</sub>* is a phase,

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- $\rightarrow p_i$  is a phase,
- $\Rightarrow \beta_i$  is a valuation of the variables,

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- $\rightarrow \gamma_i$  is a valuation of the clocks at the beginning of the interval,
- $\rightarrow$   $Y_i$  is a set of events occurring at the beginning of the interval,
- $t_i$  is a duration of the interval.

# **Semantic Property of PEA**

#### **Compositionality Lemma**

 $ho \in \textit{Runs}( \ \mathcal{A}_1 \parallel \mathcal{A}_2 \ )$ 

 $\text{iff } \rho \downarrow \mathcal{A}_1 \in \textit{Runs}(\mathcal{A}_1) \text{ and } \rho \downarrow \mathcal{A}_2 \in \textit{Runs}(\mathcal{A}_2)$ 

This lemma is at the core of a modular verification method for parallel compositions of PEA:

if a small set of parallel PEA satisfies a safety property, also a larger set of parallel PEA will satisfy it.

# **Translation of CSP**

main 
$$\stackrel{c}{=}$$
 newgoal  $\rightarrow$  start  $\rightarrow$  Drive  
Drive  $\stackrel{c}{=}$  (passed  $\rightarrow$  Drive)  $\Box$  (stop  $\rightarrow$  main)



where

$$\phi_{idle} := \neg newgoal \land \neg start \land \neg passed \land \neg stop$$

# **Translation of OZ**



where

$$\phi_{idle} := \neg newgoal \land \neg start \land \neg passed \land \neg stop$$
$$\land current = current' \land goal = goal' \land dir = dir'$$

# **Translation of DC**

Full DC cannot be translated into PEA: e.g.

$$\neg \diamondsuit( \texttt{O} ev ; \ell = 1 ; \texttt{O} ev ),$$

which means

 $\neg$  (*true*;  $\uparrow ev$ ;  $\ell = 1$ ;  $\uparrow ev$ ; *true*)

would need infinitely many clocks.
However, we can translate a useful subset: counterexample formulae.

Example 1:

 $\neg \diamond (\ \ passed ; \ \ell \leq 3 ; \ \ passed ) :$ 

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Example 1:

```
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```

Phase-Event-Automaton:



Example 2:

 $\neg \diamond ([current \neq goal]; ([current = goal] \land \ell \geq 2 \land \boxminus stop))$ 

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Phase-Event-Automaton:



#### **Automatic Verification**

Automata-theoretic approach to verification:



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Automata-theoretic approach to verification:

CODsatisfiesDC ? $\downarrow$  $\downarrow$ PEA: $\mathcal{A}(CSP) \parallel \mathcal{A}(OZ) \parallel \mathcal{A}(DC)$  $\parallel$  $\mathcal{A}_{test}(\neg DC)$ Is bad state of $\mathcal{A}_{test}(\neg DC)$ not reachable ? $\downarrow$  $\downarrow$ TCS: $\mathcal{T}(...)$ Transition Constraint System

Model checking using ARMC or SLAB or H-PILoT on TCS

## **Transition Constraint Systems**

specify states and transitions by formulas (constraints):

transition constraints relate pre- and post-state
 no notion of events, no notion of real-time

However, events and clocks can be encoded.

- ••• events: changes of Boolean variables::  $stop' \neq stop$
- clocks: real-valued variables á la Lamport:  $c' = c + \text{len} \land \text{len} > 0$

#### **Translation of PEA into TCS**

Phase-Event-Automaton:

![](_page_43_Figure_2.jpeg)

Transition Constraint System:

$$Tr \Leftrightarrow ph = 0 \land \neg passed \land c' = c + len \land ph' = 0$$
  
$$\lor ph = 0 \land passed \land c' = len \land c' \leq 3 \land ph' = 1$$
  
$$\lor ph = 1 \land \neg passed \land c' = c + len \land c' \leq 3 \land ph' = 1$$
  
$$\lor ph = 1 \land \neg passed \land c = 3 \land c' = c + len \land ph' = 0$$

# Model Checker ARMC

Podelski & Rybalchenko (since 2002)

Abstraction Refinement Model Checker

Characteristics:

- ARMC checks for reachability,
- employs the CEGAR method: counterexample-guided abstraction refinement,
- uses Craig interpolation for predicate discovery,
- evaluates implications in a decidable fragment of first-order logic: linear arithmetic over reals,
- extended with uninterpreted function symbols.
- is implemented in SICStus Prolog.

#### **Experimental Results**

Hoenicke & Maier (2005):

The formula  $Min \le current \le Max$  was checked. ARMC proved validity in 2 minutes.

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- The formula  $Min \le current \le Max$  was checked. ARMC proved validity in 2 minutes.
- → Valid for all possible choices of *Min* and *Max*.
- Property depends on real-time:
   If one DC formula is omitted ARMC found counterexample in 20 seconds.

#### **Model Checker SLAB**

Brückner, Dräger, Finkbeiner & Wehrheim (2008) Dräger, Kupriyanov, Finkbeiner & Wehrheim (2010)

Slicing Abstraction Model Checker

Characteristics:

- SLAB checks for realizability of abstract error paths
- abstracts both states and transitions,
- uses slicing of abstractions and local refinement,
- employs Craig interpolation for predicate discovery,
- checks satisfiability in a decidable fragment of first-order logic: linear arithmetic over reals,

#### **Abstract Error Paths**

![](_page_49_Figure_1.jpeg)

Does abstract error path correspond to a concrete one ?

## **Slicing Abstactions**

E.g. node elimination if Init  $\land$  Bad  $\Rightarrow$  false :

![](_page_50_Figure_2.jpeg)

## **Local Refinement**

If error path does *not* correspond to a concrete one Craig interpolation is used to discover a predicate P for node splitting.

![](_page_51_Figure_2.jpeg)

## **Termination**

![](_page_52_Figure_1.jpeg)

Checking *terminates* if

(1) the error path is realizable (system erroneous) or(2) the slice becomes empty (system correct).

![](_page_53_Figure_0.jpeg)

# **Components of Case Study**

Specification in CSP-OZ-DC J. Faber & Meyer (2006)

![](_page_54_Figure_2.jpeg)

Infinite data types:Position =  $\mathbb{R}$ , Speed =  $\mathbb{R}_{\geq 0}$ Parameters:Length, TargetSpd, ...

Hoenicke & Olderog (since 2002)

Interface:

chan updPos:[id:{ID}, pos!: Position]
chan compSBI:[loa?, sbi!: Position]

**CSP** specifies sequencing of events:

main 
$$\stackrel{c}{=}$$
 Running  $||||$  HandleEM

*Running*  $\stackrel{c}{=}$  *updPos.ID*? *pos*  $\rightarrow$  *getLOA.ID*? *loa*  $\rightarrow$  *compSBI*! *loa*? *sbi*  $\rightarrow$ 

if  $sbi \leq pos$  then ... else ...

**Object-Z** specifies state space ...

sbi : Position curPos : Position curSpd : Speed ...

... and operations:

\_\_\_\_com\_compSBI Δ(sbi) loa?, sbi! : Position sbi' = loa? - TargetSpdDist - StopDist - MaxDist sbi! = sbi'

Duration Calculus restricts timing of states and events:

• At least *updBound* seconds between two *updPos* events:

 $\neg \diamond (\ddagger updPos; \ell < updBound; \ddagger updPos)$ 

counterexample trace:

![](_page_57_Figure_5.jpeg)

	RearTrain(ID : TrainID; StartPos, StartSBI :	Position)	
	chan <i>updPos</i> :[ <i>id</i> :{ <i>ID</i> }, <i>pos</i> !: <i>Position</i> ]		
	chan <i>compSBI</i> : [ <i>loa</i> ?, <i>sbi</i> ! : <i>Position</i> ]		
CSP	 main <b><sup>c</sup> Running      HandleEM</b>		
	Running $\stackrel{c}{=}$ updPos.ID? pos $\rightarrow$ getLOA.ID? loa $\rightarrow$ compSBI! loa? sbi $\rightarrow$		
	if $sbi \le pos$ then else		
		_com_ <i>compSBI</i>	
OZ	sbi : Position	$\Delta(sbi)$	
	curPos : Position	loa?, sbi! : Position	
	curSpd : Speed	shi' - loa? - TargetSndDist - StonDist - MaxDist	
		sbi' = sbi'	
DC	$\neg \diamond$ ( $\ddagger$ updPos; $\ell <$ updBound; $\ddagger$ updPos)		

# **Properties Checked**

Meyer, Faber, Hoenicke & Rybalchenko (2008) Two trains:

- RT requirements automatically verified with ARMC. Example:
  - $\neg \diamond (\ddagger receive. EmAlert; \Box apply EB \land \Box driverAck \land reactTime < \ell)$ where *reactTime* = 8 sec.

Experimental results 2008:

4,900 locations, 99,000 transitions, 47 variables

ARMC: 216 minutes

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4,900 locations, 99,000 transitions, 47 variables ARMC: 216 minutes

Collision freedom:

2008: with manual decomposition into RT requirements

## **ETCS: More Properties Checked**

Application: ETCS with arbitrary no. of trains / segments:

Faber, Jacobs & Sofronie-Stokkermans (2010)

simplified CSP-OZ-DC model, but with 2-sorted pointer data structure:

![](_page_61_Figure_4.jpeg)

Verified: invariant property of collision freedom.

# **Data Verification with H-PILoT**

Ihlemann, S. Jacobs & Sofronie-Stokkermans (2009)

Hierarchical Proving by Instantiation in Local Theory extensions

Characteristics:

- Tool H-PILoT supports local theory extensions  $\mathcal{T}_0 \subseteq \mathcal{T}_1$ .
- Satisfiability of (quantified) formulae in extension T<sub>1</sub> is reduced to satisfiability of ground formulae in the base theory T<sub>0</sub>.
- Standard SMT solvers check satisfiability of ground formulae in the base theory  $T_0$ .
- Hierarchical reasoning / interpolation / QE for new classes of theories of data types, e.g.,
  - recursive functions,
  - many-sorted pointer structures.

# **Syspect Tool**

for modelling, specificying and verifying RTS systems with rich data. Students' work continued in AVACS project "Beyond Timed Automata". Faber, Linker, Olderog, Quesel (2011)

level	language	purpose
modelling	UML profile	model <i>M</i> of a real-time system <i>R</i> with rich data
specification	↓ CSP-OZ-DC	specification <i>S</i> of <i>R</i> as the formal semantics of <i>M</i>
verification	↓ PEA ↓	operational semantics O of S
	TCS	representation of <i>O</i> as input for verification engines like ARMC, SLAB, or H-PILoT

# **Tool Chain for Syspect Verification**

![](_page_64_Figure_1.jpeg)

## **Further Developments**

- **Explicit Durations**
- Parallel Composition

## **Translatable DC Classes**

(1) Full DC cannot be translated into PEA.

(2) Counterexample formulae: powerset construction takes care of overlapping timed phases and yields deterministic PEA

PhD thesis Hoenicke (2006)

 (3) Explicit Durations: translation (2) extended by stop watches
 In discrete time setting: Availability Automata
 Hoenicke, Meyer & Olderog (2010)

# **Explicit Durations**

... can express timed availability requirements:

 $\int$  (speed  $\geq$  target)  $\geq$  0.9  $\cdot \ell$ 

"For at least 90% of the time interval, the train meets its target speed."

... correspond to integrators (stop watches), a source of undecidability separating TA and LHA.

New translations to automata for reachability analysis:

Multi-Priced Time Automata

continuous time

Availability Automata (new)

discrete time

## **Availablity Automata**

Availabilities in discrete setting (words).

regular availability expressions (rea)  $\mapsto$  availability automata (aa)

**Example:**  $((up + down)^*.\checkmark)_{\{up\}\geq\frac{1}{3}}$ 

![](_page_68_Figure_4.jpeg)

availability counter x with test  $c(x) = (\{up\} \ge \frac{1}{3})$ 

Kleene theorem. A language is recognized by a flat rae *if and only if* it is accepted by a simple aa.

Powerset construction. Every simple aa can be *determinized* and *complemented* by inverting final states.

# **Avoiding Product Construction**

Large COD specifications yield (too) many parallel PEA.

ETCS Emergency Messages: collision freedom for two trains

Full COD specifications yields 18 parallel PEAs.

![](_page_69_Figure_4.jpeg)

# **Avoiding Product Construction**

Large COD specifications yield (too) many parallel PEA.

ETCS Emergency Messages: collision freedom for two trains

Full COD specifications yields 18 parallel PEAs.

![](_page_70_Figure_4.jpeg)

PhD thesis Faber (2011)

![](_page_70_Figure_6.jpeg)

#### **Structural Transformations**

For real-time systems with data (modelled by Extended Timed Automata), we

- isolate conditions (like independence of transitions or memorylessness of locations),
- which enable property-preserving transformations that replace parallel by sequential composition and eliminate loops.
- This results in systems that allow for an easier conceptual and automatic analysis.

More details: see lecture by Mani Swaminathan.


Semantic methods + automatic verification techniques

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